

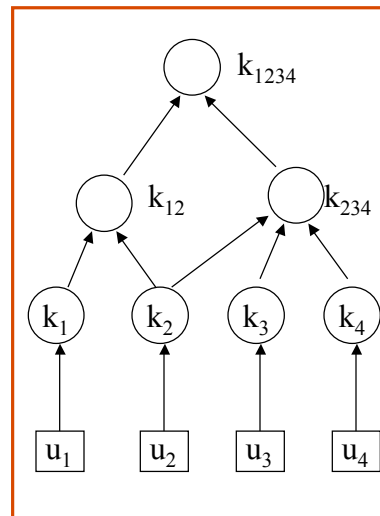


# CSC 774 Network Security

## Topic 7.2 Group Key Distribution -- Logical Key Hierarchy

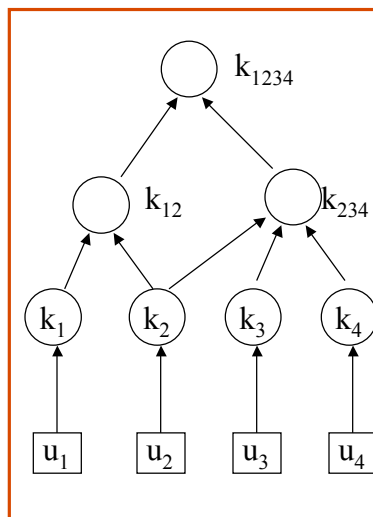
## Key Graph

- A key graph is a DAG with two types of nodes
  - **U-nodes**: represent users
    - Each u-node has one or more outgoing edges, but no incoming edges
  - **K-nodes**: represent keys
    - Each k-node has one or more incoming edges
    - **Root**: the k-node without outgoing edge



## Key Graph (Cont'd)

- A key graph  $G$  specifies a secure group
  - The key corresponding to the root  $k$ -node is used as the group key.
- Join
- Leave

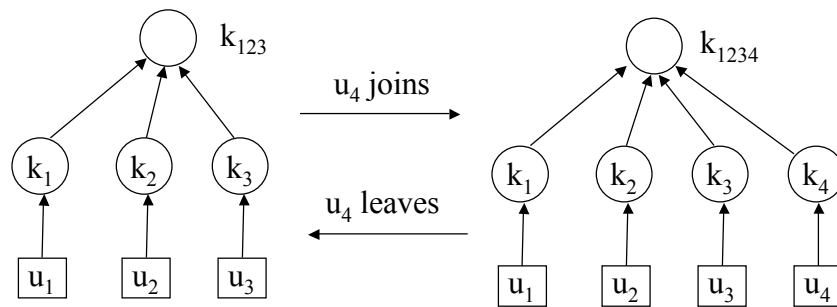


## Key Graph (Cont'd)

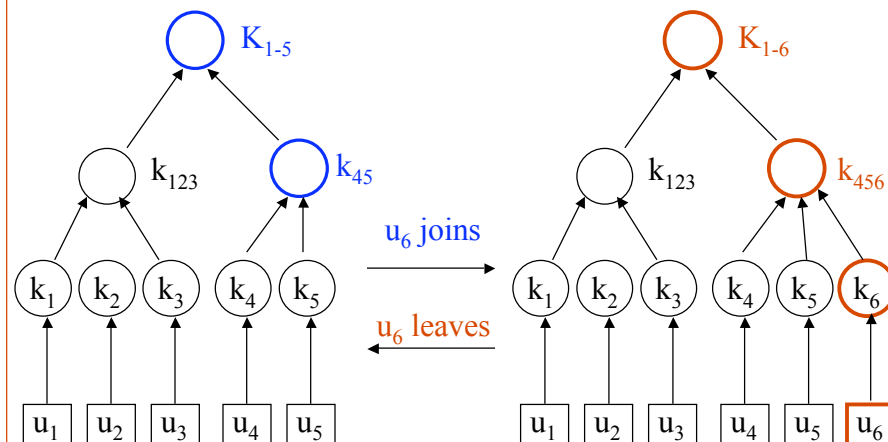
- Special cases
  - Key star
  - Key tree
    - Also known as Logical Key Hierarchy (LKH)

## Key Star

- Naïve group key distribution
  - Join
  - Leave



## Key Tree

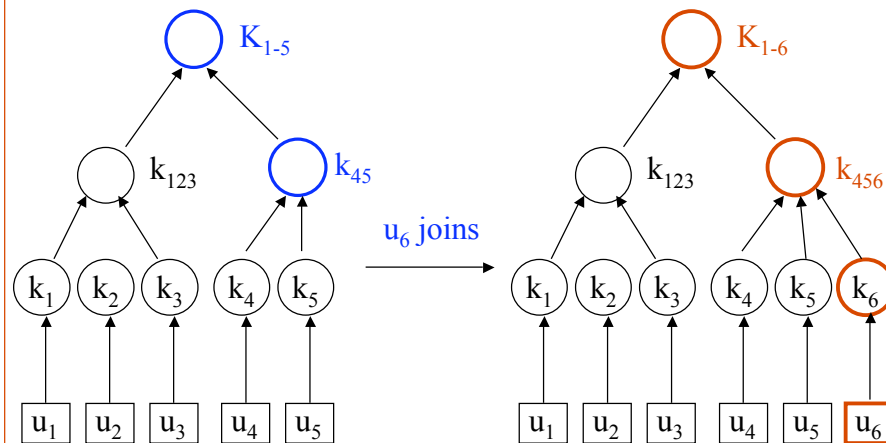


## Joining A Key Tree

- User-oriented rekey
  - Idea: send each user precisely the new keys needed by the user
  - Approach
    - For each k-node with updated key ( $k \rightarrow k'$ ), construct a message by encrypting the new key and all its ancestors by the old key ( $k$ )
    - Send this message to the subset of users that precisely needs these keys
    - Send one rekey message to the joining user with all the new keys encrypted by the joining user's individual key

## Joining A Key Tree (Cont'd)

- What are the rekey messages?

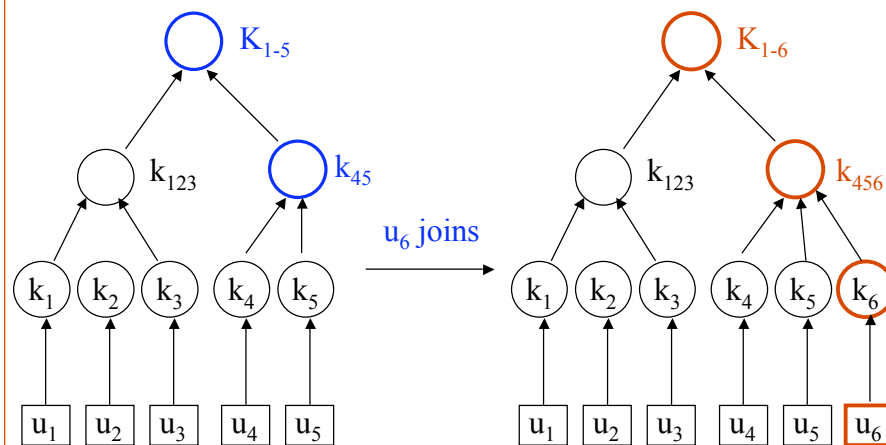


## Joining A Key Tree (Cont'd)

- Key-oriented rekey
  - Idea: **each key is encrypted individually**
  - Approach:
    - For updated k-node ( $k \rightarrow k'$ ), construct two messages
      - New key ( $k'$ ) encrypted with the old key ( $k$ )
        - » Send to the users that share  $k$
      - New key encrypted with the joining user's individual key
        - » Send to the joining member
    - Combine the rekey messages

## Joining A Key Tree (Cont'd)

- What are the rekey messages?

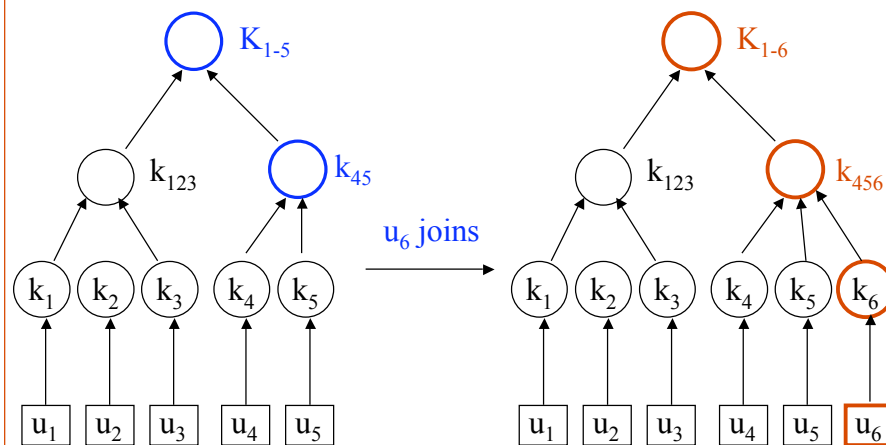


## Joining A Key Tree (Cont'd)

- Group-oriented rekey
  - Idea: prepare rekey message for the entire group
  - Approach:
    - Similar to the key-oriented rekey, but merge all the messages for old members into one message
    - Reduce communication overhead if multicast (or broadcast) is available
    - Not all the contents are necessary for each (old) user

## Joining A Key Tree (Cont'd)

- What are the rekey messages?

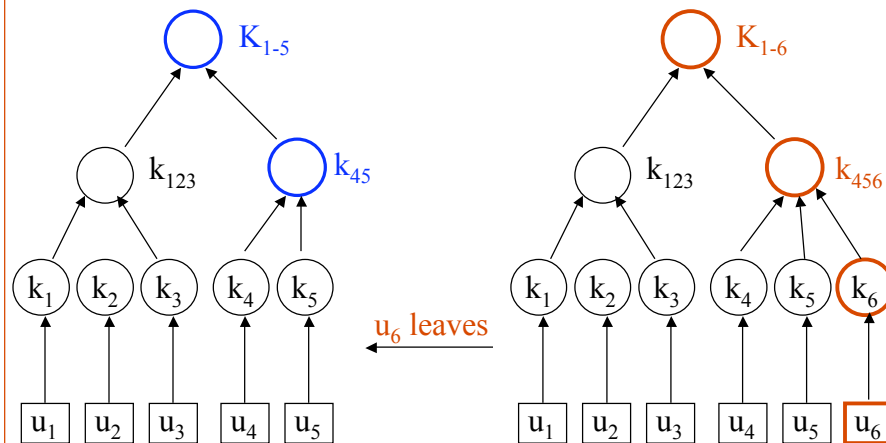


## Leaving A Key Tree

- User-oriented rekey
  - Idea: each user gets a rekey message with all keys it needs encrypted with a key it holds
  - Approach:
    - Update the keys in the path from the removed user to the root
    - For each updated k-node  $x$  ( $k \rightarrow k'$ ), and for each unchanged child  $y$ , construct a rekey message by encrypting the new keys of  $x$  and all its ancestors's new keys by the key  $K$  of  $y$
    - Multicast this message to the users that have  $K$ .

## Leaving A Key Tree (Cont'd)

- What are the rekey messages?

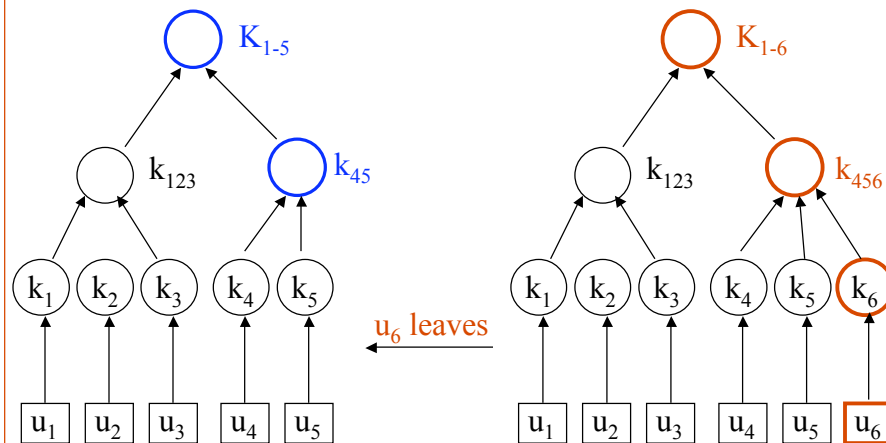


## Leaving A Key Tree (Cont'd)

- Key-oriented rekey
  - Idea: encrypt each new key individually
  - Approach:
    - Update the keys in the path from the removed user to the root
    - For each updated k-node  $x$  ( $k \rightarrow k'$ ), for each non-updated child  $y$  of  $x$ , use  $y$ 's key  $K$  to encrypt  $k'$ , use  $k$  to encrypt  $x$ 's ancestor's key, ...
    - Send this message to the users having  $K$

## Leaving A Key Tree (Cont'd)

- What are the rekey messages?





## Leaving A Key Tree (Cont'd)

- Group-oriented rekey
  - Idea: construct a single rekey message for the entire group.
  - Approach:
    - Similar to key-oriented rekey, but combine all rekey messages into one

## Leaving A Key Tree (Cont'd)

- What are the rekey messages?

