Efficient, Compromise Resilient and Append-only Cryptographic Schemes for Secure Audit Logging

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Abstract. Due to the forensic value of audit logs, it is vital to provide *compromise resiliency* and *append-only* properties in a logging system to prevent active attackers. Unfortunately, existing symmetric secure logging schemes are not publicly verifiable and cannot address applications that require public auditing (e.g., public financial auditing), besides being vulnerable to certain attacks and dependent on continuous trusted server support. Moreover, Public Key Cryptography (PKC)-based secure logging schemes require Expensive Operations (ExpOps) that are costly for both loggers and verifiers, and thus are impractical for computation-intensive environments.

In this paper, we propose a new class of secure audit logging scheme called \underline{Log} Forward-secure and Append-only Signature (LogFAS). LogFAS achieves the most desirable properties of both symmetric and PKC-based schemes. LogFAS can produce publicly verifiable forward-secure and append-only signatures without requiring any online trusted server support or time factor. Most notably, LogFAS is the only PKC-based secure audit logging scheme that achieves the high verifier computational and storage efficiency. That is, LogFAS can verify L log entries with always a small-constant number of ExpOps regardless of the value of L. Moreover, each verifier stores only a small and constant-size public key regardless of the number of log entries to be verified or the number of loggers in the system. In addition, a LogFAS variation allows fine-grained verification of any subset of log entries and fast detection of corrupted log entries. All these properties make LogFAS an ideal scheme for secure audit logging in computation-intensive applications.

Keywords: Secure audit logging; applied cryptography; forward security; signature aggregation.

1 Introduction

Audit logs have been used to track important events such as user activities and program execution in modern computer systems, providing invaluable information about

the state of the systems (e.g., intrusions, crashes). Due to their forensic value, audit logs are an attractive target for attackers. Indeed, an experienced attacker may erase the traces of her malicious activities from the logs, or modify the log entries to implicate other users after compromising the system. Therefore, ensuring the integrity, authenticity and accountability of audit logs in the presence of attackers is critical for any modern computer system [9, 20, 23, 27].

There are straightforward techniques to protect audit logs from active adversaries: (i) Using a tamper resistant hardware on each logging machine to prevent the adversary from modifying audit logs and (ii) transmitting each log entry as soon as it is generated to a remote trusted server. Unfortunately, these approaches have significant limitations as identified in [9, 19, 20]: First, it is impractical to assume both the presence and the "bug-freeness" of a tamper resistant hardware on all types of platforms (e.g., wireless sensors [18], commercial off-the-shelf systems [7]) [17, 20]. Second, it is difficult to guarantee timely communication between each logging machine and the remote trusted server in the presence of active adversaries [11, 19, 27].

Limitations of Previous Cryptographic Log Protection Techniques: Cryptographic mechanisms can protect the integrity of audit logs without relying on such techniques. In these settings, the log verifiers might not be available to verify the log entries once they are generated. Hence, a logger may have to accumulate log entries for a period of time. If the adversary takes full control of the logging machine in this duration, no cryptographic mechanism can prevent her from modifying the post-attack log entries. However, the integrity of log entries accumulated before the attack should be protected (i.e., *forward-security* property) [1,7,9,12,17,19,20,27]. Furthermore, this protection should not only guarantee the integrity of individual log entries but also the integrity of the log stream as a whole. That is, no selective deletion or truncation of log entries should be possible (i.e., *append-only* (*aggregate*) property [17,18,20]). Forward-secure and aggregate signatures (e.g., [17,18,20,27,28]) achieve forward-security and append-only properties simultaneously.

Pioneering forward-secure audit logging schemes [6,7,23] rely on symmetric primitives such as Message Authentication Code (MAC) to achieve computationally efficient integrity protection. However, the symmetric nature of these schemes does not allow public verifiability. This property is necessary for applications such as financial auditing applications where financial books of publicly held companies need to be verified by the current and potential future share holders [12,20]. Furthermore, symmetric schemes require online remote trusted server support, which entails costly maintenance and attracts potential attacks besides being a potential single-point of failures. Finally, these schemes are shown to be vulnerable against the truncation and delayed detection attacks [19,20] (no append-only property).

To mitigate the above problems, several PKC-based secure audit logging schemes have been proposed (e.g., [12, 17, 18, 20, 27]). These schemes are publicly verifiable and do not require an online TTP support. However, they are costly for loggers (except for BAF [27]) and extremely costly for the log verifiers. Second, to verify a particular log entry, all these schemes [17–19, 27] force log verifiers to verify the entire set of log entries, which entails a linear number of Expensive Operations (ExpOps)¹, and failure

¹ For brevity, we denote an expensive cryptographic operation such as modular exponentiation or pairing as an ExpOp.

Table 1. Comparison of LogFAS schemes and their counterparts for performance, applicability, availability and security parameters

C-:4:-		PKC-based					
Criteria Computational		LogFAS FSSAgg/iFssAgg AR BM BLS BA		BAF	Logcrypt	[7,23]	
	Sig&Upd (per item)	ExpOp	ExpOp		H	ExpOp	H
On-	Ver, (L items)	$ExpOp + O(L \cdot H)$	$O(L \cdot (ExpOp +$		Op + I	H))	$O(L \cdot H)$
line	Subset ver $(l' < L)$	$ ExpOp + O(l' \cdot H) $	O(2l'(ExpOp + H)) Not immuta		immutable	$O(l' \cdot H)$	
	Efficient Search	Available	Not Available				-
Key Generation (Offline)		$O(L \cdot ExpOp)$					$O(L \cdot H)$
Storage	Verifier	K	$O(S \cdot K)$ $O(L \cdot S) K $			$O(S \cdot K)$	
1	Signer	$O(L \cdot (D + K))$	$O(L \cdot$	D) + K	1	$O(L \cdot K)$	$O(L \cdot K)$
Cor	nmunication	$O(L \cdot D)$					
	ic Verifiability	Y		N			
Offline Server		Y		N			
Immediate Verification		Y	Y				N
Immediate Detection		Y	Y			N	
Truncation Resilience		Y		Ŋ	(N	N

LogFAS is the only PKC-based secure audit logging scheme that can verify O(L) items with a small-constant number of ExpOps; all other similar schemes require O(L) ExpOps. Similarly, LogFAS is the only one achieving constant number of public key storage (with respect to both number of data items and log entries to be verified) on the verifier side, while all other schemes incur either linear or quadratic storage overhead (S, |D|, |K| denote the number of signers in the system, the approximate bit lengths of a log entry and the bit length of a keying material, respectively). At the same time, LogFAS is the only scheme that enables truncation-free subset verification and sub-linear search simultaneously.

of this verification does not give any information about which log entry(ies) is (are) responsible for the failure.

Our Contribution: In this paper, we propose a new secure audit logging scheme, which we call <u>Log Forward-secure and Append-only Signature</u> (LogFAS). We first develop a main LogFAS scheme, and then extend it to provide additional capabilities. The desirable properties of LogFAS are outlined below. The first three properties show the efficiency of LogFAS compared with their PKC-based counterparts, while the other three properties demonstrate the applicability, availability and security advantages over their symmetric counterparts. Table 1 summarizes the above properties and compares LogFAS with its counterparts.

- 1. Efficient Log Verification with O(1) ExpOp: All existing PKC-based secure audit log-ging schemes (e.g., [12,17–20,27,28]) require O(L · (ExpOp + H)) to verify L log entries, which make them costly. LogFAS is the first PKC-based secure audit logging scheme that achieves signature verification with only a small-constant number of ExpOps (and O(L) hash operations). That is, LogFAS can verify L log entries with only a small-constant number of ExpOps regardless of the value of L. Therefore, it is much more efficient than all of its PKC-based counterparts, and is also comparably efficient with symmetric schemes (e.g., [7, 18, 23]) at the verifier side.
- 2. Efficient Fine-grained Verification and Change Detection: LogFAS allows fine-grained verification with advantages over iFssAgg [20], the only previous solution for fine-grained verification:
 - (i) Unlike iFssAgg schemes [20], LogFAS prevents the truncation attack² in the presence of individual signatures without doubling the verification cost.

The truncation attack is a special type of deletion attack, in which the adversary deletes a continuous subset of tail-end log entries. This attack can be prevented via "all-or-nothing" property [18]: The adversary either should remain previously

- (ii) LogFAS can verify any selected subset with l' < L log entries with a small-constant number of ExpOps, while iFssAgg schemes require O(2l')ExpOps.
- (iii) LogFAS can identify the corrupted log entries with a *sub-linear* number of ExpOps when most log entries are intact. In contrast, iFssAgg schemes always require a linear number of ExpOps.
- 3. <u>Verifier Storage Efficiency with O(1) Overhead</u>: Each verifier in LogFAS only stores one public key independent of the number of loggers or the number of log entries to be verified. Therefore, it is the most verifier-storage-efficient scheme among all existing PKC-based alternatives. This enables verifiers to handle a large number of log entries and/or loggers simultaneously without facing any storage problem.
- 4. <u>Public Verification</u>: Unlike the symmetric schemes (e.g., [7, 18, 23]), LogFAS can produce publicly verifiable signatures, and therefore it can protect applications requiring public auditing (e.g., e-voting, financial books) [12, 20].
- 5. <u>Independence of Online Trusted Server</u>: LogFAS schemes do not require online trusted server support to enable log verification. Therefore, LogFAS schemes achieve high availability, and are more reliable than the previous schemes that require such support (e.g., [7, 23, 28]).
- 6. <u>High Security</u>: We prove LogFAS to be forward-secure existentially unforgeable against adaptive chosen-message attacks in Random Oracle Model (ROM) [4]. Furthermore, unlike some previous symmetric schemes [7, 23], LogFAS schemes are also secure against both truncation and delayed detection attacks.

2 Preliminaries

Notation. || denotes the concatenation operation. |x| denotes the bit length of variable $x. x \overset{\$}{\leftarrow} \mathcal{S}$ denotes that variable x is randomly and uniformly selected from set \mathcal{S} . For any integer $l, (x_0, \ldots, x_l) \overset{\$}{\leftarrow} \mathcal{S}$ means $(x_0 \overset{\$}{\leftarrow} \mathcal{S}, \ldots, x_l \overset{\$}{\leftarrow} \mathcal{S})$. We denote by $\{0, 1\}^*$ the set of binary strings of any finite length. H is an ideal cryptographic hash function, which is defined as $H: \{0, 1\}^* \to \{0, 1\}^{|H|}; |H|$ denotes the output bit length of H. $\mathcal{A}^{\mathcal{O}_0, \ldots, \mathcal{O}_i}(\cdot)$ denotes algorithm \mathcal{A} is provided with oracles $\mathcal{O}_0, \ldots, \mathcal{O}_i$. For example, $\mathcal{A}^{Scheme.Sig_{sk}}(\cdot)$ denotes that algorithm \mathcal{A} is provided with a signing oracle of signature scheme Scheme under private key sk.

Definition 1. A signature scheme SGN is a tuple of three algorithms (Kg, Sig, Ver) defined as follows:

- $(sk, PK) \leftarrow SGN.Kg(1^{\kappa})$: Key generation algorithm takes the security parameter 1^{κ} as the input. It returns a private/public key pair (sk, PK) as the output.
- $\sigma \leftarrow SGN.Sig(sk, D)$: The signature generation algorithm takes sk and a data item D as the input. It returns a signature σ as the output (also denoted as $\sigma \leftarrow SGN.Sig_{sk}(D)$).
- $c \leftarrow SGN.Ver(PK, D, \sigma)$: The signature verification algorithm takes PK, D and σ as the input. It outputs a bit c, with c=1 meaning valid and c=0 meaning invalid.

accumulated data intact, or should not use them at all (she cannot selectively delete/modify any subset of this data [20]). LogFAS is proven to be secure against the truncation attack in Section 5.

Definition 2. Existential Unforgeability under Chosen Message Attack (EU-CMA) experiment for SGN is as follows:

Experiment $Expt_{SGN}^{EU\text{-}CMA}(\mathcal{A})$

$$(sk, PK) \leftarrow SGN.Kg(1^{\kappa}), (D^*, \sigma^*) \leftarrow \mathcal{A}^{SGN.Sig_{sk}(\cdot)}(PK),$$

If $SGN.Ver(PK, D^*, \sigma^*) = 1$ and D^* was not queried, return 1, else, return 0.

 $\begin{array}{l} \text{EU-CMA-advantage of \mathcal{A} is $Adv_{SGN}^{EU-CMA}(\mathcal{A}) = Pr[Expt_{SGN}^{EU-CMA}(\mathcal{A}) = 1]$.} \\ \text{EU-CMA-advantage of SGN is $Adv_{SGN}^{EU-CMA}(t,L,\mu) = \max_{\mathcal{A}} \{Adv_{SGN}^{EU-CMA}(\mathcal{A})\}$, where} \end{array}$

EU-CMA-advantage of SGN is $Adv_{SGN}^{EU-CMA}(t, L, \mu) = \max_{\mathcal{A}} \{Adv_{SGN}^{EU-CMA}(\mathcal{A})\}$, where the maximum is over all \mathcal{A} having time complexity t, making at most L oracle queries, and the sum of lengths of these queries being at most μ bits.

LogFAS is built on the Schnorr signature scheme [24]. It also uses an Incremental Hash function \mathcal{IH} [3] and a generic signature scheme SGN (e.g., Schnorr) as building blocks. Both Schnorr and \mathcal{IH} require that $H:\{0,1\}^* \to \mathbb{Z}_q^*$ is a random oracle.

Definition 3. The Schnorr signature scheme is a tuple of three algorithms (Kg, Sig, Ver) behaving as follows:

- $(y,\langle p,q,\alpha,Y\rangle)\leftarrow Schnorr.Kg(1^\kappa)$: Key generation algorithm takes 1^κ as the input. It generates large primes q and p>q such that q|(p-1), and then generates a generator α of the subgroup G of order q in \mathbb{Z}_p^* . It also generates $(y\overset{\$}\leftarrow\mathbb{Z}_q^*,\ Y\leftarrow\alpha^y \bmod p)$, and returns private/public keys $(y,\langle p,q,\alpha,Y\rangle)$ as the output.
- $(s, R, e) \leftarrow Schnorr.Sig(y, D)$: Signature generation algorithm takes private key y and a data item D as the input. It returns a signature triplet (s, R, e) as follows: $R \leftarrow \alpha^r \mod p$, $e \leftarrow H(D||R)$, $s \leftarrow (r e \cdot y) \mod q$, where $r \stackrel{\$}{\leftarrow} \mathbb{Z}_q^s$.
- $c \leftarrow Schnorr.Ver(\langle p,q,\alpha,Y\rangle,D,\langle s,R,e\rangle)$: Signature verification algorithm takes public key $\langle p,q,\alpha,Y\rangle$, data item D and signature $\langle s,R,e\rangle$ as the input. It returns a bit c, with c=1 meaning valid if $R=Y^e\alpha^s \mod p$, and with c=0 otherwise.

Definition 4. Given a large random integer q and integer L, incremental hash function family \mathcal{IH} is defined as follows: Given a random key $z=(z_0,\ldots,z_{L-1})$, where $(z_0,\ldots,z_{L-1}) \overset{\$}{\leftarrow} \mathbb{Z}_q^*$ and hash function H, the associated incremental hash function $\mathcal{IH}_z^{q,L}$ takes an arbitrary data item set D_0,\ldots,D_{L-1} as the input. It returns an integer $T \in Z_q$ as the output,

Algorithm
$$\mathcal{IH}_z^{q,L}(D_0,\ldots,D_{L-1})$$

 $T \leftarrow \sum_{j=0}^{L-1} H(D_j)z_j \bmod q$, return T .

Target Collision Resistance (TCR) [5] of \mathcal{IH} relies on the intractability of *Weighted Sum of Subset (WSS) problem* [3, 13] assuming that H is a random oracle.

Definition 5. Given $\mathcal{IH}_z^{q,L}$, let \mathcal{A}_0 be an algorithm that returns a set of target messages, and \mathcal{A}_1 be an algorithm that returns a bit. Consider the following experiment: Experiment $\operatorname{Expt}_{\mathcal{IH}_z^{q,L}}^{TCR}(\mathcal{A}=(\mathcal{A}_0,\mathcal{A}_1))$

$$(D_0, \dots, D_{L-1}) \leftarrow \mathcal{A}_0(L), z = (z_0, \dots, z_{L-1}) \stackrel{\$}{\leftarrow} \mathbb{Z}_q^*,$$

 $T \leftarrow \mathcal{IH}_z^{q,L}(D_0, \dots, D_{L-1}), (D_0^*, \dots, D_{L-1}^*) \leftarrow \mathcal{A}_1(D_0, \dots, D_{L-1}, T, \mathcal{IH}_z^{q,L})$

If $T = \mathcal{IH}_z^{q,L}(D_0^*, \dots, D_{L-1}^*) \wedge \exists j \in \{0, \dots, L-1\} : D_j^* \neq D_j$, return 1, else, return 0.

TCR-advantage of \mathcal{A} is $Adv_{\mathcal{IH}_z^{q,L}}^{TCR}(\mathcal{A}) = Pr[Expt_{\mathcal{IH}_z^{q,L}}^{TCR}(\mathcal{A}) = 1]$. TCR-advantage of $\mathcal{IH}_z^{q,L}$ is $Adv_{\mathcal{IH}_z^{q,L}}^{TCR}(t) = \max_{\mathcal{A}} \{Adv_{\mathcal{IH}_z^{q,L}}^{TCR}(\mathcal{A})\}$, where the maximum is over all \mathcal{A} having time complexity t.

3 Syntax and Models

LogFAS is a Forward-secure and Append-only Signature (FSA) scheme, which combines *key-evolve* (e.g., [2, 15]) and *signature aggregation* (e.g., [8]) techniques. Specifically, LogFAS is built on the Schnorr signature scheme [21, 24], and it integrates forward-security and signature aggregation strategies in a novel and efficient way. That is, different from previous approaches (e.g., [17–20, 23, 27, 28]), LogFAS introduces verification with a constant number of ExpOps, selective subset verification and sublinear search properties via incremental hashing [3] and masked tokens in addition to the above strategies.

Before giving more details, we briefly discuss the *append-only* signatures. A forward-secure and aggregate signature scheme is an *append-only* signature scheme if no message can be re-ordered or selectively deleted from a given stream of messages, while new messages can be appended to the stream [18, 20]. In Section 5, we prove that Log-FAS is an append-only signature scheme.

Definition 6. A FSA is comprised of a tuple of three algorithms (Kg, FASig, FAVer) behaving as follows:

- $(sk, PK) \leftarrow FSA.Kg(1^{\kappa}, L)$: The key generation algorithm takes the security parameter 1^{κ} and the maximum number of key updates L as the input. It returns a private/public key pair (sk, PK) as the output.
- $(sk_{j+1}, \sigma_{0,j}) \leftarrow FSA.FASig(sk_j, D_j, \sigma_{0,j-1})$: The forward-secure and appendonly signing algorithm takes the current private key sk_j , a new message D_j to be signed and the append-only signature $\sigma_{0,j-1}$ on the previously signed messages (D_0, \ldots, D_{j-1}) as the input. It computes an append-only signature $\sigma_{0,j}$ on (D_0, \ldots, D_j) , evolves (updates) sk_j to sk_{j+1} , and returns $(sk_{j+1}, \sigma_{0,j})$ as the output.
- $c \leftarrow FSA.FAVer(PK, \langle D_0, \dots, D_j \rangle, \sigma_{0,j})$: The forward-secure and append-only verification algorithm takes $PK, \langle D_0, \dots, D_j \rangle$ and their corresponding $\sigma_{0,j}$ as the input. It returns a bit c, with c=1 meaning valid, and c=0 otherwise.

In LogFAS, private key sk is a vector, whose elements are comprised of specially constructed Schnorr private keys and a set of tokens. These tokens later become the part of append-only signature σ accordingly. The public key PK is a system-wide public key that is shared by all verifiers, and is comprised of two long-term public keys. Details are given in Section 4.

3.1 System Model

LogFAS system model is comprised of a *Key Generation Center (KGC)* and multiple signers (i.e., logging machines that could be compromised) and verifiers. As in forward-secure stream integrity model (e.g., [7, 17, 18]), signers honestly execute the scheme until they are compromised by the adversary. Verifiers may be *untrusted*.

The KGC executes LogFAS.Kg once offline before the deployment, and distributes a distinct private key/token set (auxiliary signature) to each signer, and two long-term public keys to all verifiers. After the deployment, a signer computes the forward-secure and append-only signature of log entries with LogFAS.FASig, and verifiers can verify the signature of any signer with LogFAS.FAVer via two public keys without communicating with KGC (constant storage overhead at the verifier side).

In LogFAS, the same logger computes the append-only signature of her own log entries. Note that this form of signature computation is ideal for the envisioned secure audit logging applications, since each logger is only responsible for her own log entries.

3.2 Security Model

A FSA scheme is proven to be ForWard-secure Existentially Unforgeable against Chosen Message Attack (FWEU-CMA) based on the experiment defined in Definition 7. In this experiment, \mathcal{A} is provided with two types of oracles that she can query up to L messages in total as follows:

 \mathcal{A} is first provided with a *batch signing oracle* $FASig_{sk}(\cdot)$. For each batch query j, \mathcal{A} queries $FASig_{sk}(\cdot)$ on a set of message \overrightarrow{D}_j of her choice once. $FASig_{sk}(\cdot)$ returns a forward-secure and append-only signature $\sigma_{0,j}$ under sk by aggregating σ_j (i.e., the current append-only signature) on \overrightarrow{D}_j with the previous signature $\sigma_{0,j-1}$ on $\overrightarrow{D}_0,\ldots,\overrightarrow{D}_{j-1}$ that \mathcal{A} queried. Assume that \mathcal{A} makes i batch queries (with $0 \leq l \leq L$ individual messages) as described the above until she decides to "break-in".

 \mathcal{A} then queries the Break-in oracle, which returns the remaining L-l private keys to \mathcal{A} (if l=L Break-in rejects the query).

Definition 7. FWEU-CMA experiment is defined as follows:

Experiment $Expt_{FSA}^{FWEU-CMA}(A)$

$$(sk, PK) \leftarrow FSA.Kg(1^{\kappa}, L), (\overrightarrow{D}^*, \sigma^*) \leftarrow \mathcal{A}^{FASig_{sk}(\cdot), Break-in}(PK),$$

If $FSA.FAVer(PK, \overrightarrow{D}^*, \sigma^*) = 1 \land \forall I \subseteq \{0, \dots, l\}, \overrightarrow{D}^* \neq ||_{k \in I} \overrightarrow{D}_k$, return 1, else, return 0.

$$\mbox{FWEU-CMA-advantage of } \mathcal{A} \mbox{ is } Adv_{FSA}^{FWEU-CMA}(\mathcal{A}) = Pr[Expt_{FSA}^{FWEU-CMA}(\mathcal{A}) = 1].$$

FWEU-CMA-advantage of FSA is $Adv_{FSA}^{FWEU-CMA}(t,L,\mu) = \max_{\mathcal{A}} \{Adv_{FSA}^{FWEU-CMA}(\mathcal{A})\}$, where the maximum is over all \mathcal{A} having time complexity t, making at most L oracle queries, and the sum of lengths of these queries being at most μ bits.

The above experiment does not implement a random oracle for \mathcal{A} explicitly. However, we still assume the *Random Oracle Model (ROM)* [4], since Schnorr signature scheme [24] on which LogFAS is built requires the ROM. Note that this experiment also captures the *truncation attacks*:

- (i) The winning condition of \mathcal{A} subsumes the truncation attack in addition to data modification. That is, \mathcal{A} wins the experiment when she either modifies a data item or keeps data items intact but outputs a valid signature on a subset of a given batch query (i.e., she splits an append-only signature without knowing its individual signatures).
- (ii) LogFAS uses a standard signature scheme SGN to prevent truncation attacks by computing signatures of counter values. Resilience against the traditional data forgery (without truncation) relies on EU-CMA property of Schnorr and target collision-freeness of \mathcal{IH} . In Theorem 1, we prove that a successful truncation attack against LogFAS is equivalent to breaking SGN, and a successful data modification (including re-ordering) against LogFAS is equivalent to breaking Schnorr or \mathcal{IH} .

4 LogFAS Schemes

In this section, we first present the intuition and detailed description of LogFAS, and then describe a LogFAS variation that has additional capabilities.

4.1 LogFAS Scheme

All existing FSA constructions [17–20, 27] rely on a direct combination of an aggregate signature (e.g., [8]) and a forward-secure signature (e.g., [1, 15]). Therefore, the resulting constructions simultaneously inherit all overheads of their base primitives: (i) Forward-secure signatures on individual data items, which are done separately from the append-only design, force verifiers to perform O(l) ExpOps. (ii) These schemes either eliminate ExpOps from the logging phase with pre-computation but incur quadratic storage overhead to the verifiers (e.g., [27]), or require ExpOps in the logging phase for each log entry and incur linear storage overhead to the verifiers (e.g., [12, 17, 20]).

The above observations inspired us to design cryptographic mechanisms that can verify *the integrity of entire log entry set once directly* (preserving forward-security), instead of checking the integrity of each data item individually, though the signing operations have to be performed on individual data items. That is, instead of verifying each item one-by-one with the corresponding public key(s), verify all of them via a *single set of aggregated cryptographic components* (e.g., tokens as auxiliary signatures). These mechanisms also achieve constant storage overhead at the verifier side³.

We achieve these goals with a provable security by using Schnorr signature and incremental hash \mathcal{IH} as follows:

- a) To compute a forward-secure and append-only Schnorr signature, we aggregate each individual signature s_l on D_l with the previous aggregate signature as $s_{0,l} \leftarrow s_{0,l-1} + s_l \bmod q$, $(0 < l \le L-1, s_{0,0} = s_0)$. This is done by using a distinct private key pair (r_j, y_j) for $j = 0, \ldots, L-1$ on each data item.
- b) Despite being forward-secure, the above construction still requires an ExpOp for each data item. To verify the signature on D_0, \ldots, D_l with only a small-constant number of ExpOps, we introduce the notion of *token*.

In LogFAS, each Schnorr private y_j is comprised of a random key pair (a_j,d_j) for $j=0,\ldots,L-1$. Random key a_j is mutually blinded with another random factor x_j and also a long-term private key b for $j=0,\ldots,L-1$. The result of these blinding

³ In all existing forward-secure and/or aggregate (append-only) logging schemes (e.g., [7,12,17,19,20,27]), the signer side storage overhead is dominated by the accumulated logs, which already incur a linear storage overhead.

operations is called *auxiliary signature* (token) z_j , which can be kept publicly without revealing information about (a_j, x_j) and also can be authenticated with the long-term public key B by all verifiers. Furthermore, these masked tokens $z = z_0, \ldots, z_l$ also serve as a one-time initialization key for the incremental hash as $\mathcal{IH}_z^{q,l}$ (Definition 4), which enable verifiers to reduce the integrity of each D_j into the integrity of a final tag $z_{0,l}$. This operation preserves the integrity of each D_j and verifiability of each z_j (via public key B) without ExpOps.

c) To verify $(s_{0,l}, z_{0,l})$ via B in an aggregate form, verifiers also aggregate tokens R_j as $R_{0,l} \leftarrow \prod_{j=0}^l R_j \mod p$, where p a large prime on which the group was constructed. However, initially, $(s_{0,l}, R_{0,l}, z_{0,l})$ cannot be verified directly via B, since the reduction operations introduce some extra verification information. LogFAS handles this via *auxiliary signature* (token) $M'_{0,l}$ that bridges $(s_{0,l}, R_{0,l}, z_{0,l})$ to B. That is, the signer computes an aggregate token $M'_{0,l} \leftarrow M'_{0,l-1} M_l^{e_j} \mod p$, where $0 < l \le L-1$ and $M_{0,0} = M_0$), along with $s_{0,l}$ in the signing process. During verification, this aggregate token eliminates the extra terms and bridges $(s_{0,l}, R_{0,l}, z_{0,l})$ with B.

This approach allows LogFAS to compute publicly verifiable signatures with only one ExpOp per-item, and this signature can be verified with only a small-constant number of ExpOps by storing only two public keys at the verifier side (regardless of the number of signers). This is much more efficient than all of its PKC-based counterparts, and also is as efficient as the symmetric schemes at the verifier side.

The detailed description of LogFAS algorithms is given below:

- 1) $LogFAS.Kg(1^{\kappa}, L)$: Given 1^{κ} , generate primes q and p > q such that q|(p-1), and then generate a generator α of the subgroup G of order q in \mathbb{Z}_p^* .
- a) Generate $(b \stackrel{\$}{\leftarrow} \mathbb{Z}_q^*, B \leftarrow \alpha^{b^{-1}} \mod p)$ and $(\widehat{sk}, \widehat{PK}) \leftarrow SGN.Kg(1^\kappa)$. Systemwide private key of KGC is $\overline{sk} \leftarrow (b, \widehat{sk})$. This private key is used to compute the private key of all signers in the system. System-wide public key of all verifiers is $PK \leftarrow \{p, q, \alpha, B, \widehat{PK}, L\}$. This public key can verify any valid signature generated by a legitimate signer.
- b) Generate $(r_j, a_j, d_j, x_j) \stackrel{\$}{\leftarrow} \mathbb{Z}_q^*$ for $j = 0, \dots, L-1$. The private key of signer ID_i is $sk \leftarrow \{r_j, y_j, z_j, M_j, R_j, \beta_j\}_{j=0}^{L-1}$, where
 - Generate the Schnorr private key of each ID_i as $y_j \leftarrow a_j d_j \mod q$. Generate the masked token of ID_i as $z_j \leftarrow (a_j x_j)b \mod q$, which is used for integrity reduction at the verification phase.
 - $R_j \leftarrow \alpha^{r_j} \mod p$, $M_j \leftarrow \alpha^{x_j-d_j} \mod p$. Each R_j serves as a part of Schnorr signature and it is aggregated by the verifier upon its receipt. M_j is the aggregate token and is aggregated by the signer during the logging process.
 - $\beta_j \leftarrow SGN.Sig(\hat{sk}, H(ID_i||j))$. Note that each β_j is kept secret initially, and then released as a part of a signature publicly.
- 2) $LogFAS.FASig(\langle r_l, y_l, z_l, M_l, R_l, \beta_l \rangle, D_l, \sigma_{0,l-1})$: Given $\sigma_{0,l-1}$ on D_0, \ldots, D_{l-1} , compute $\sigma_{0,l}$ on D_0, \ldots, D_l as follows,
- a) $e_l \leftarrow H(D_l||l||z_l||R_l)$, $M'_l \leftarrow M_l^{e_l} \mod p$, $s_l \leftarrow r_l e_l y_l \mod q$,
- b) $s_{0,l} \leftarrow s_{0,l-1} + s_l \mod q$, $(0 < l \le L 1, s_{0,0} = s_0)$,

- c) $M'_{0,l} \leftarrow M'_{0,l-1}M'_l \mod p$, $(0 < l \le L-1, M'_{0,0} = M_0)$,
- d) $\sigma_{0,l} \leftarrow \{s_{0,l}, M'_{0,l}, \beta_l, R_j, e_j, z_j\}_{j=0}^l$ and erase $(r_l, y_l, s_{0,l-1}, s_l, \beta_{l-1})$.
- 3) $LogFAS.FAVer(PK, \langle D_0, \ldots, D_l \rangle, \sigma_{0,l})$:
- a) If SGN. $Ver(\widehat{PK}, H(ID_i||l), \beta_l) = 0$ then return 0, else continue,
- b) If $\prod_{j=0}^{l} R_j \mod p = M'_{0,l} \cdot B^{z_{0,l}} \cdot \alpha^{s_{0,l}} \mod p$ holds return 1, else return 0, where $z_{0,l} = \mathcal{IH}^{q,l}_{z_0,\ldots,z_l}(D_0||w||z_0||R_0,\ldots,D_l||w||z_l||R_l)$.

4.2 Selective Verification with LogFAS

All the previous FSA constructions (e.g., [17–19, 27, 28]) verify the set of log entries via only the final aggregate signature to prevent the truncation attack and save the storage. However, this approach causes performance drawbacks: (i) The verification of any subset of log entries requires the verification of the entire set of log entries (i.e., always O(L) ExpOps for the subset verification). (ii) The failure of signature verification does not give any information about which log entries were corrupted.

Ma et al. proposed immutable-FssAgg (iFssAgg) schemes in [20] to allow fine-grained verification without being vulnerable to truncation attacks. However, iFssAgg schemes double the signing/verifying costs of their base schemes. In addition, even if the signature verification fails due to only a few corrupted log entries (i.e., accidentally damaged entry(ies)), detecting which log entry(ies) is (are) responsible for the failure requires verifying each individual signature.

LogFAS can address the above problems via a simple variation without incurring any additional costs: The signer keeps *all* signatures and tokens in their individual forms (including s_j for $j=0,\ldots,l$) without aggregation. The verifiers can aggregate them according to their needs by preserving the security and verifiability. This offers performance advantages over iFssAgg schemes [20]:

- (i) LogFAS protects the number of log entries via pre-computed tokens β_0,\ldots,β_l , and therefore individual signatures can be kept without a truncation risk. This eliminates the necessity of costly immutability strategies used in iFssAgg schemes [20]. Furthermore, a verifier can selectively aggregate any subset of l' < l log entries and verify them by performing only a small-constant number of ExpOps as in the original LogFAS. This is much more efficient than the iFssAgg schemes, which require O(2l') ExpOps.
- (ii) LogFAS can use a recursive subset search strategy to identify corrupted log entries causing the verification failure faster than linear search⁴. That is, the set of log entries is divided into subsets along with their corresponding individual signatures. Each subset is then independently verified by LogFAS.AVer via its corresponding aggregate signature, which is efficiently computed from individual signatures. Subsets returning 1 are eliminated from the search, while each subset returning 0 is again divided into subsets and verified by LogFAS.AVer as described. This subset search continues recursively until all the corrupted log entries are identified.

⁴ Note that the previous PKC-based audit logging schemes *cannot* use such a recursive subset search strategy to identify corrupted log entries with a sub-linear number ExpOps, since they always require linear number of ExpOps to verify a given subset from the entire log entry set (in contrast to LogFAS that requires O(1)ExpOp to verify a given subset).

The above strategy can quickly identify the corrupted entries when most log entries are intact. For instance, if only one entry is corrupted, it can identify the corrupted entry by performing $(2\log_2 l)$ ExpOps + O(l) hash operations. This is much faster than linear search used in the previous PKC-based schemes, which always requires O(l) ExpOps + O(l) hash operations.

Recursive subset strategy remains more efficient than linear search as long as the number of corrupted entries c satisfies $c \leq \frac{l}{2\log_2 l}$. When $c > \frac{l}{2\log_2 l}$, depending on c and the distribution of corrupted entries, recursive subset search might be more costly than linear search. To minimize the performance loss in such an inefficient case, the verifier can switch from recursive subset search to the linear search if the recursive division and search step continuously returns 0 for each verified subset. The verifier can ensure that the performance loss due to an inefficient case does not exceed the average gain of an efficient case by setting the maximum number of recursive steps to be executed to $l'/2 - \log_2 l'$ for each subset with l' entries.

5 Security Analysis

We prove that LogFAS is a FWEU-CMA signature scheme in Theorem 1 below.

Theorem 1 $Adv_{LogFAS}^{FWEU\text{-}CMA}(t,L,\mu)$ is bounded as follows,

$$\begin{split} Adv_{LogFAS}^{FWEU\text{-}CMA}(t,L,\mu) & \leq L \cdot Adv_{Schnorr}^{EU\text{-}CMA}(t',1,\mu') + \\ & Adv_{SGN}^{EU\text{-}CMA}(t'',L,\mu'') + Adv_{\mathcal{IH}_{z}^{q,L}}^{TCR}(t'''), \end{split}$$

where
$$t' = O(t) + L \cdot O(\kappa^3)$$
 and $\mu' = \mu/L$.

The proof of the theorem can be found in our accompanying technical report [29].

Remark 1 Another security concern in audit logging is *delayed detection* identified in [19]. In delayed detection, log verifiers cannot detect whether the log entries are modified until an online TTP provides auxiliary keying information to them. LogFAS does not rely on an online TTP support or time factor to achieve the signature verification, and therefore it is not prone to delayed detection.

6 Performance Analysis and Comparison

In this section, we present the performance analysis of LogFAS and compare it with previous schemes.

Computational Overhead: From a verifier's perspective, LogFAS requires only a small-constant number of modular exponentiations regardless of the number of log entries to be verified. Therefore, it is much more efficient than all PKC-based schemes, which require one modular exponentiation (or a pairing) per log entry. Besides, it does not double the verification cost to prevent the truncation attacks, providing further efficiency over iFssAgg schemes [20]. The verification of subsets from these entries with LogFAS is also much more efficient than all of its counterparts.

Table 2. Execution time (in ms) comparison of LogFAS and its counterparts

Criteria		PKC-based						
		LogFAS	FssAgg (l) / iFssAgg (l')			Logcrypt	BAF	Sym.
		$ (l=10^4, l' < l) $	BLS / i	BM / i	AR/i	18.71		
Off.	$Kg, L = 10^4$	5.06×10^4	3.3×10^{3}	8.8×10^{4}	1.7×10^{5}	2.6×10^{4}	4×10^4	<u>2</u> 0
	Sig&Upd(1)	1.2	1.8 / 3.6	13.1 / 26.2	28 / 56	2.05	0.007	0.004
Onl.	$l' = 10^2$	72.87	4.8×10^{3}	1.8×10^{3}	1.6×10^{5}	1.4×10^{3}	0.2×10^{3}	0.2
OIII.	Ver. $l' = 10^3$	75.2	4.8×10^{4}	1×10^4	1.8×10^{5}	1.5×10^{4}	2.05×10^{3}	2
	$l = 10^4$	98.12	2.6×10^{5}	4.7×10^{4}	1.9×10^{5}	1.4×10^{5}	2.04×10^{4}	19.9

From a logger's perspective, LogFAS is also more efficient than its PKC-based counterparts with the exception of BAF.

We prototyped our schemes and their counterparts on a computer with an Intel(R) Xeon(R)-E5450 3GHz CPU and 4GB RAM running Ubuntu 9.04. We tested LogFAS, BAF [27], FssAgg-BLS [18], Logcrypt (with DSA), and the symmetric schemes (e.g., [7, 18, 23]) using the MIRACL library [25], and FssAgg-AR/BM using the NTL library [26] 5 . Table 2 compares the computational cost of LogFAS with its counterparts numerically in terms of their execution times (in ms). The execution time differences with LogFAS and its PKC-based counterparts grow linearly with respect to the number of log entries to be verified. Initially, the symmetric schemes are more efficient than all PKC-based schemes, including ours. However, since the verification operations of LogFAS are dominated by H, their efficiency become comparable with symmetric schemes as the number of log entries increases (e.g., $l = 10^4$).

Figure 1 and Figure 2 further compare LogFAS and previous schemes that allow public verification in terms of signature generation and verification times as the number of log entries increases. These figures demonstrate that LogFAS is the most verifier computationally efficient scheme among all these choices. It is also more efficient than its counterparts for the signature generation with the exception of BAF.

All PKC-based schemes require O(L) ExpOps in the key generation phase.

Signature/Key/Data Storage and Transmission Overheads:

LogFAS is a verifier storage friendly scheme; it requires each verifier to store only two public keys and an index along with system-wide parameters (e.g., |q| + |4p|), regardless of the number of signers or the number of log entries to be verified.

In LogFAS, the append-only signature size is |q|. The key/token and data storage overheads on the logger side are linear as O(L(5|q|+2|p|))+O(l|D|) (assuming SGN is chosen as Schnorr [24]). LogFAS transmits a token set along with each data item requiring O(l(|q|+|p|+|D|)) transmission in total. The fine-grain verification introduces O(l') extra storage/communication overhead due to the individual signatures.

From a verifier's perspective, LogFAS is much more storage efficient than all existing schemes, which require either $O(L \cdot S)$ storage (e.g., FssAgg-BLS [18] and BAF [27]), or O(S) storage (e.g., [7,12,17,20,23]). From a logger's perspective, all the

⁵ Suggested bit lengths to achieve 80-bit security for each compared schemes are as follows (based on the parameters suggested by Lenstra et al. in [16] and Ma et al. in [17,18]): Large primes (|p|=2048, |q|=1600) for LogFAS and Logcrypt, primes (|p'|=512, |q'|=160) for BAF and FssAgg-BLS, (|n'|=1024, z=160) for FssAgg-AR and FssAgg-BM, where n' is Blum-Williams integer [17].

 $^{^6}$ To achieve TCR property for \mathcal{IH} , LogFAS uses relatively larger modulo sizes than its counterparts. However, since LogFAS requires only a small-constant number of ExpOps for the signature verification and a single ExpOp for the signature generation, the effect of large modulo size over its performance is negligible.

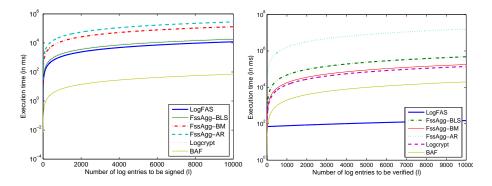


Fig. 1. Signing time comparison of LogFAS and **Fig. 2.** Verification time comparison of LogFAS its counterparts (in ms) and its counterparts (in ms)

Table 3. Key size, signature size and storage overheads of LogFAS and previous schemes

		PKC-based						
Criteria		LogFAS	FssAgg Schemes [19] BLS [18] BM [17]		9,20] AR [17]	Logcrypt [12]	Sym. [18, 22, 23]	
Sig.	Key size	O(L)(q + p)	3 q'	q'	n' z	3 n'	q' + p'	H
	Sig. size	O(l)(q + p)	q'	p'	n'	n'	2 q'	H
	Storage	O(L+l)(q + p)	4 q'	2 q' + 3 p'	n' l	4 n'	O(L)(q' + p')	O(V) H
Vor	Key size	q + 4 p	2 p'	q'	n' z	3 n'	2 q' + p'	H
	Storage	q + 4 p	$O(L \cdot S)(2 p')$	$O(L \cdot S) q' $	O(S) n' z	O(S) 3n'	O(L)(q' + p')	O(S) H

The values in this table are simplified by omitting some constant/neglibigle terms. For instance, the overhead of data items to be transmitted are the same for all compared schemes and therefore are omitted.

compared schemes both accumulate (store) and transmit linear number of data items (i.e., O(l)|D|) until their verifiers become available to them. This dominates the main storage and communication overhead for these schemes. In addition to this, LogFAS requires linear key storage overhead at the logger side, which is slightly less efficient than [17, 18, 27]. LogFAS with fine-grained verification and its counterpart iFssAgg schemes [20] both require linear key/signature/data storage/transmission overhead.

Availability, Applicability and Security: The symmetric schemes [7, 23] are not publicly verifiable and also require online server support to verify log entries. Furthermore, they are vulnerable to both truncation and delayed detection attacks [19,20] with the exception of FssAgg-MAC [18]. In contrast, PKC-based schemes [12, 17–20] are publicly verifiable without requiring online server support, and they are secure against the truncation and delayed detection attacks, with the exception of Logcrypt [12].

7 Related Work

Most closely related are those forward-secure audit logging schemes [6,7,12,17–20,23, 27]. The comparison of these schemes with LogFAS has been presented in Section 6.

Apart from the above schemes, there is a set of works complementary to ours. Itkis [14] proposed cryptographic tamper resistance techniques that can detect tampering even if all the keying material is compromised. LogFAS can be combined with Itkis model as any forward-secure signature [14]. Yavuz et al. [28] proposed a Hashbased Forward-Secure and Aggregate Signature Scheme (HaSAFSS) for unattended

wireless sensor networks, which uses timed-release encryption to achieve computational efficiency. Davis et al. proposed time-scoped search techniques on encrypted audit logs [10]. There are also authenticated data structures that can be used for audit logging in distributed systems [9]. LogFAS can serve as a digital signature primitive needed by these constructions.

8 Conclusion

In this paper, we proposed a new forward-secure and append-only audit logging scheme called LogFAS. LogFAS achieves public verifiability without requiring any online trusted server support, and is secure against truncation and delayed detection attacks. LogFAS is much more computationally efficient than all existing PKC-based alternatives, with a performance comparable to symmetric schemes at the verifier side. LogFAS is also the most verifier storage efficient scheme among all existing alternatives. Last, a variation of LogFAS enables selective subset verification and efficient search of corrupted log entries. Overall, our comparison with the existing schemes shows that LogFAS is an ideal choice for secure audit logging by offering high efficiency, security, and public verifiability simultaneously for real-life applications.

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